

1

$\alpha = 90^\circ + \frac{m(\widehat{A})}{2}$

[AD] çizilirse açıortay olur.

D : İç teğet çemberin merkezi, iç açıortayların kesişme noktasıdır.

2

$\alpha = 90^\circ - \frac{m(\widehat{A})}{2}$

[AD] çizilirse açıortay olur.

D : Dış teğet çemberlerden birinin merkezidir.

3

$\alpha = \frac{m(\widehat{A})}{2}$

[AD] çizilirse açıortay olur.

1

2

$|AH| = |BK| = |CL|$

3

$|DE| + |DF| + |DK| = a$

4

$|DE| + |DF| + |DK| = |AH|$

1

$b = a + c$

2

$a + b + c = 360^\circ$

3

4

$a + b = 180^\circ$

5  $x + y = 90^\circ$  ise x ve y tümler açıdır.

6  $x + y = 180^\circ$  ise x ve y bütünler açıdır.

7  $1^\circ = 60' = 3600'' \Rightarrow \frac{D}{180^\circ} = \frac{R}{\pi}$

## ÜÇGENLER - 1

**ÜÇGENDE AÇILAR**

**EŞKENAR ÜÇGEN**

**DOĞRUDA AÇILAR**

**DİK ÜÇGEN VE TRİGONOMETRİ-İ**

**İKİZKENAR ÜÇGEN**

1

i. Yükseklik  $\rightarrow h_a$   
ii. Açıortay  $\rightarrow n_A$   
iii. Kenarortay  $\rightarrow V_a$   
iv. İkizkenarlık  $\rightarrow |AB| = |AC|$

$|AH| = h_a = n_A = V_a$

$|AB| = |AC|$

Dört bilgidен ikisi varsa, diğer ikisi de vardır.

2

$h_b = h_c$

3

$|DE| + |DF| = |AB| = |AC|$

4

$n_B = n_C$

5

$|DE| + |DF| = |BH| = |CK|$

6

$V_b = V_c$

1

Muhteşem üçlü

Pisagor Bağıntısı

$b^2 = a^2 + c^2$

2 Öklid Bağıntıları

$h^2 = p \cdot k$   
 $c^2 = p \cdot a$   
 $b^2 = k \cdot a$   
 $a \cdot h = b \cdot c$

3 Kenarlarına Göre Özel Üçgenler

- 3 - 4 - 5 üçgeni
- 5 - 12 - 13 üçgeni
- 8 - 15 - 17 üçgeni
- 7 - 24 - 25 üçgeni
- k - 2k - k√5 üçgeni

4

$k, 2k, k\sqrt{3}$

$k, k, k\sqrt{2}$

$k, k, k\sqrt{3}$

$h, 4h$

5

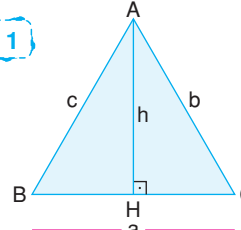
$\sin \alpha = \frac{c}{b}$   
 $\cos \alpha = \frac{a}{b}$   
 $\tan \alpha = \frac{c}{a}$   
 $\cot \alpha = \frac{a}{c}$

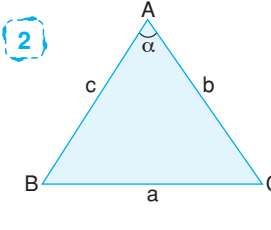
6 Kosinüs Teoremi

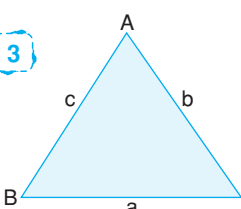
$a^2 = b^2 + c^2 - 2 \cdot b \cdot c \cdot \cos \alpha$

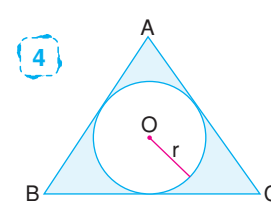
7 Sinüs Teoremi

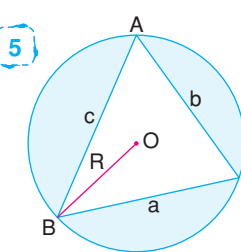
$\frac{a}{\sin \widehat{A}} = \frac{b}{\sin \widehat{B}} = \frac{c}{\sin \widehat{C}} = 2r$

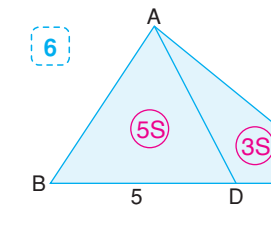
**1**   $A(\widehat{ABC}) = \frac{a \cdot h}{2}$

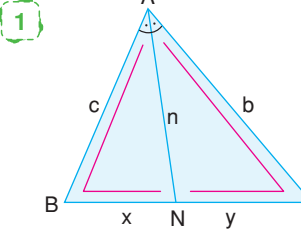
**2**   $A(\widehat{ABC}) = \frac{1}{2} \cdot b \cdot c \cdot \sin \alpha$

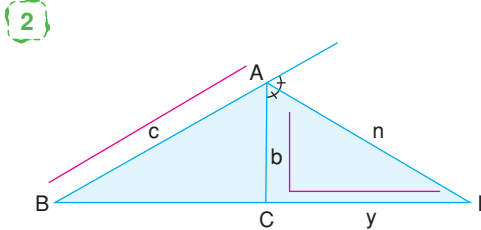
**3** 

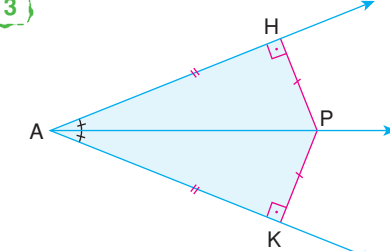
**4**   $A(\widehat{ABC}) = u \cdot r$   
(u : üçgenin çevresinin yarısı)

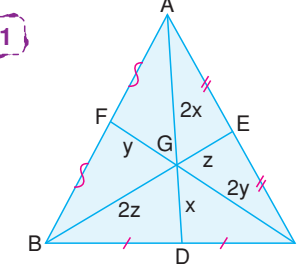
**5**   $A(\widehat{ABC}) = \frac{a \cdot b \cdot c}{4R}$

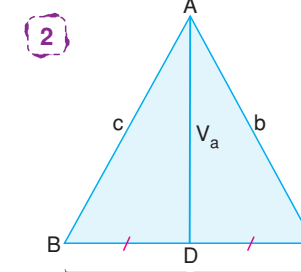
**6** 

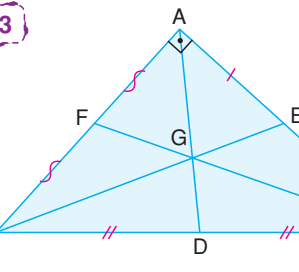
**1**   $\frac{c}{x} = \frac{b}{y}$   
 $n^2 = b \cdot c - x \cdot y$

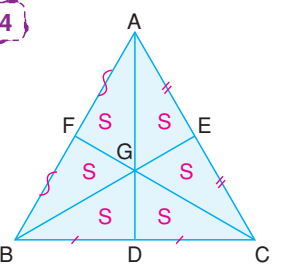
**2**   $\frac{c}{x} = \frac{b}{y}$   
 $n^2 = x \cdot y - b \cdot c$

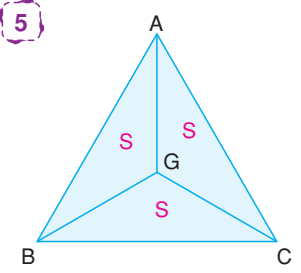
**3** 

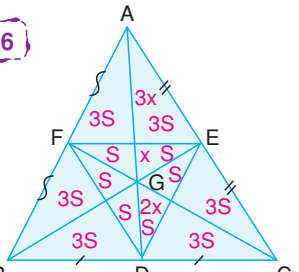
**1** 

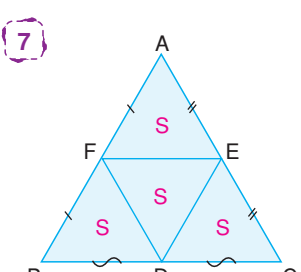
**2**   $2V_a^2 = b^2 + c^2 - \frac{a^2}{2}$

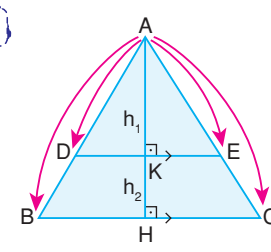
**3**   $|AD| = V_a$   
 $|BE| = V_b$   
 $|CF| = V_c$   
 $5V_a^2 = V_b^2 + V_c^2$

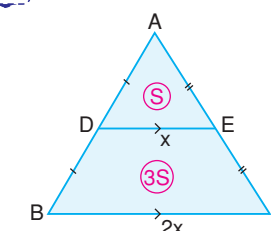
**4** 

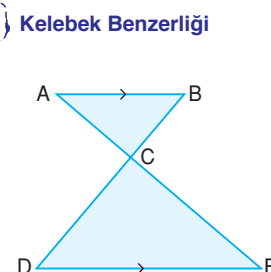
**5** 

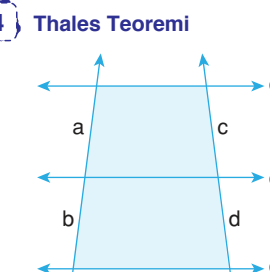
**6** 

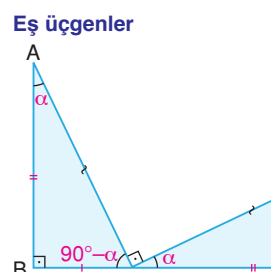
**7** 

**1**   $\widehat{ADE} \sim \widehat{ABC}$   
 $k = \frac{|ADI|}{|ABI|} = \frac{|AEI|}{|ACI|} = \frac{|DEI|}{|BCI|} = \frac{h_1}{h_1 + h_2}$   
 $k^2 = \frac{A(\widehat{ADE})}{A(\widehat{ABC})}$

**2** Temel Benzerlik 

**3** Kelebek Benzerliği   $\widehat{ABC} \sim \widehat{EDC}$

**4** Thales Teoremi   $d_1 \parallel d_2 \parallel d_3$   
 $\frac{a}{b} = \frac{c}{d}$

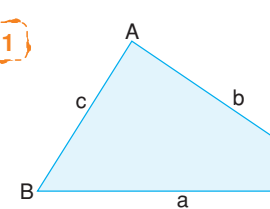
**5** Eş üçgenler   $k = 1$  ise üçgenler eştir.  
 $\widehat{ABC} \cong \widehat{CED}$

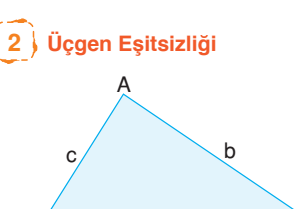
**ÜÇGENLER-2**

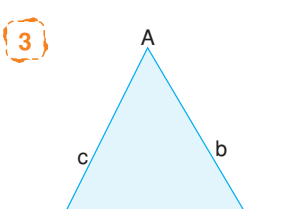
ÜÇGENDE ALAN

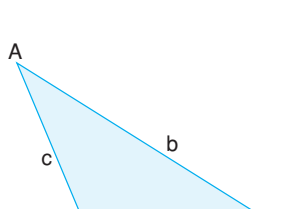
ÜÇGENDE BENZERLİK

ÜÇGENDE AÇI-KENAR BAĞINTILARI

**1**   $m(\widehat{A}) > m(\widehat{B}) > m(\widehat{C})$  ise  
 $a > b > c$   $h_a < h_b < h_c$   
 $n_A < n_B < n_C$   $V_a < V_b < V_c$

**2** Üçgen Eşitsizliği   $|b - c| < a < b + c$   
 $|a - c| < b < a + c$   
 $|a - b| < c < a + b$

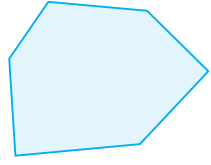
**3**   $\alpha < 90^\circ$   
 $b^2 < a^2 + c^2$

  $\alpha > 90^\circ$   
 $b^2 > a^2 + c^2$

AÇIORTAY

KENARORTAY

n kenarlı bir çokgenin,



- Bir köşesinden  $n - 3$  tane köşegen çizilir.
- Bir köşesinden çizilen köşegenler  $n - 2$  tane üçgen oluşturur.
- Köşegen sayısı  $\frac{n(n-3)}{2}$  dir.
- İç açı toplamı  $(n - 2) \cdot 180^\circ$  dir.
- Dış açı toplamı  $360^\circ$  dir.

KONVEKS ÇOKGEN

DÜZGÜN ÇOKGEN

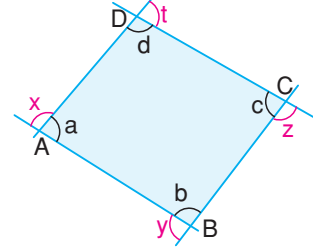
ÇOKGENLER

ÇOKGENLER VE DÖRTGENLER - 1

DÖRTGENLER

DELTOİD

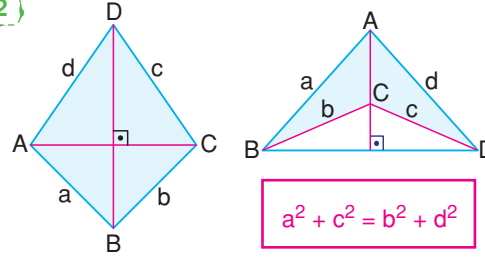
1



$$a + b + c + d = 360^\circ$$

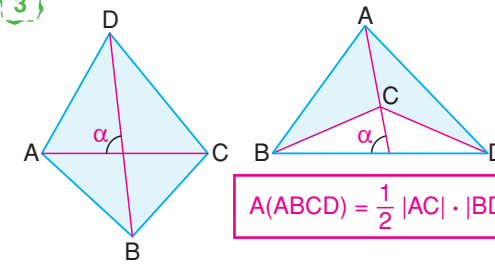
$$x + y + z + t = 360^\circ$$

2



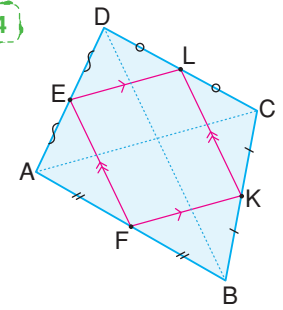
$$a^2 + c^2 = b^2 + d^2$$

3



$$A(ABCD) = \frac{1}{2} |AC| \cdot |BD| \cdot \sin \alpha$$

4

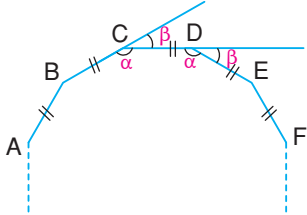


EFKL paralelkenar

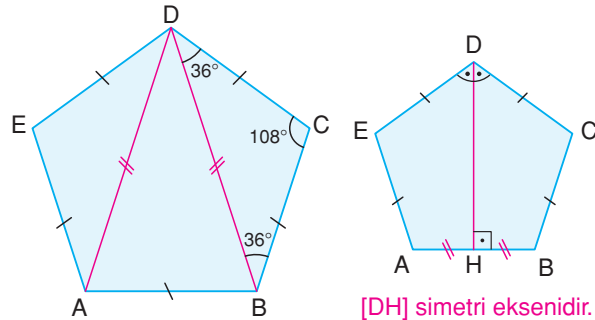
- $\angle(EFKL) = |AC| + |BD|$
- $A(EFKL) = \frac{A(ABCD)}{2}$

1 n kenarlı bir düzgün çokgenin,

- Bir dış açısının ölçüsü  $\beta = \frac{360^\circ}{n}$
- Bir iç açısının ölçüsü  $\alpha = \frac{(n-2) \cdot 180^\circ}{n}$
- $\alpha + \beta = 180^\circ$

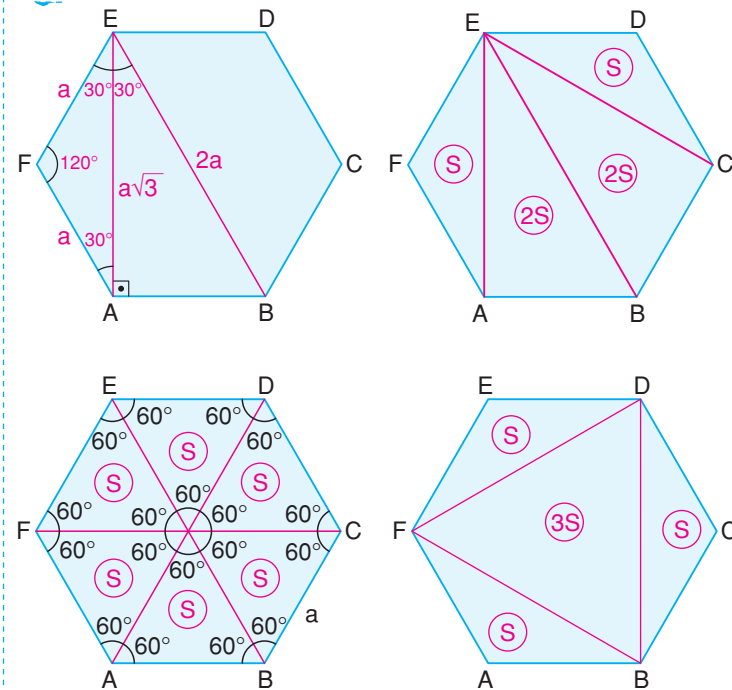


2 Düzgün Beşgen



[DH] simetri eksenidir.

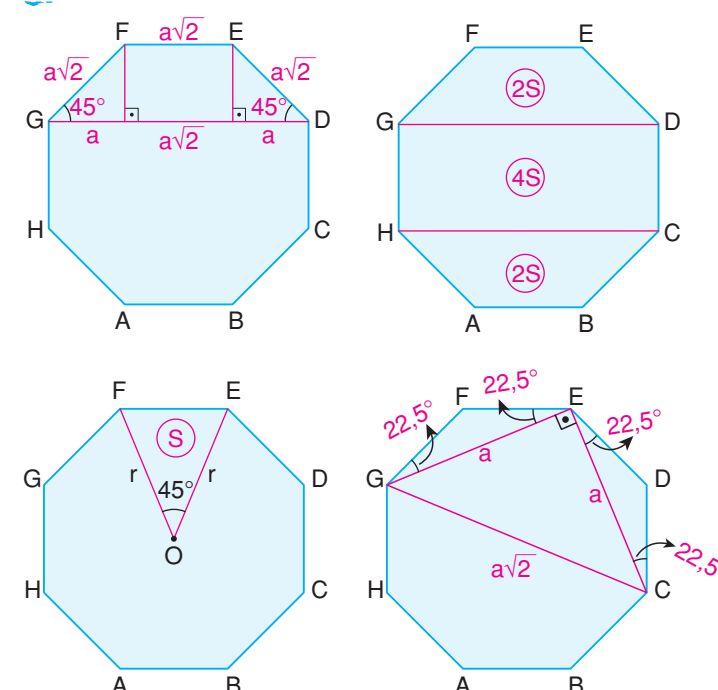
3 Düzgün Altıgen



$$S = \frac{a^2 \sqrt{3}}{4}$$

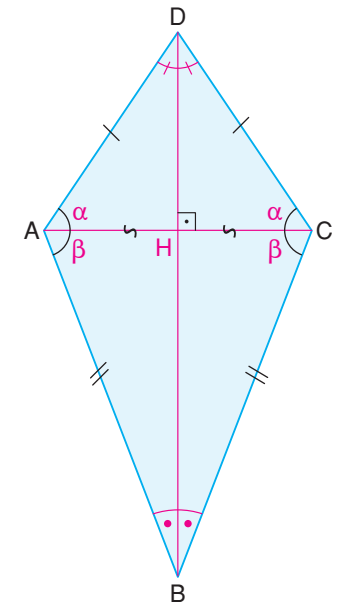
$$A(ABCDEF) = 6S$$

4 Düzgün Sekizgen



$$S = \frac{1}{2} \cdot r \cdot r \cdot \frac{\sqrt{2}}{2}$$

$$A(ABCDEFGH) = 8S$$



- Köşegenler dik kesişir.
- [BD] açıortay ve simetri eksenidir.
- $m(\widehat{BAD}) = m(\widehat{BCD})$
- $|AH| = |HC|$
- $A(ABCD) = \frac{|AC| \cdot |BD|}{2}$

**ALAN**

1 Köşegenler birbirini ortalar

2

3

4

5  $A(\widehat{APB}) = \frac{A(ABCD)}{2}$

6  $S_1 + S_3 = S_2 + S_4 = \frac{A(ABCD)}{2}$

7

8

9  $|DF| + |BH| = |AE| + |CK|$   
 $[AE] \parallel [DF] \parallel [BH] \parallel [CK]$

**ALAN**

$A(ABCD) = a \cdot ha = b \cdot hb$

$A(ABCD) = a \cdot b \cdot \sin \alpha$

**Dört kenarı birbirine eşit paralelkenardır.**

• Köşegenler dik kesişir.  
• Köşegenler açıortaydır.

**ALAN**

$A(ABCD) = a \cdot h$

1  $|EF| = \frac{a+c}{2}$

2

3

4  $A(\widehat{ADE}) = \frac{A(ABCD)}{2}$

5 İkizkenar yamukta köşegenler eşittir.

6  $h^2 = a \cdot c$

**ALAN**

$A(ABCD) = \left(\frac{a+c}{2}\right) \cdot h$

**ÇOKGENLER VE DÖRTGENLER 2**

**PARALELKENAR**

**EŞKENAR DÖRTGEN**

**Bütün açıları 90° olan paralelkenardır.**

1 Köşegenler eşittir.  
 $A(ABCD) = a \cdot b$

2  $x^2 + z^2 = y^2 + t^2$

**DİKDÖRTGEN**

**Bütün kenarları eşit olan dikdörtgendir.**

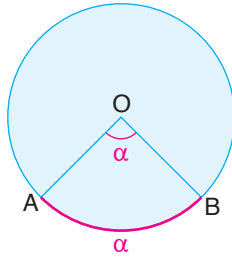
• Köşegenler dik kesişir.  
• Köşegenler açıortaydır.

$A(ABCD) = a^2$

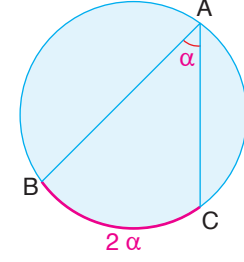
**KARE**

**YAMUK**

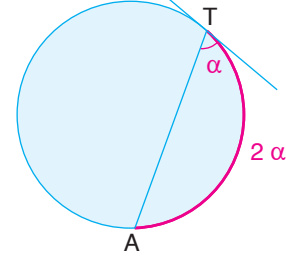
## 1 Merkez Açısı



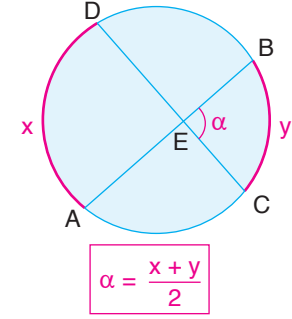
## 2 Çevre Açısı



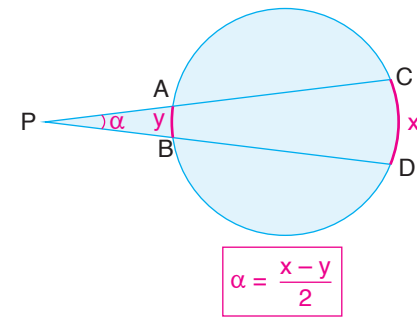
## 3 Teğet - Kiriş Açısı



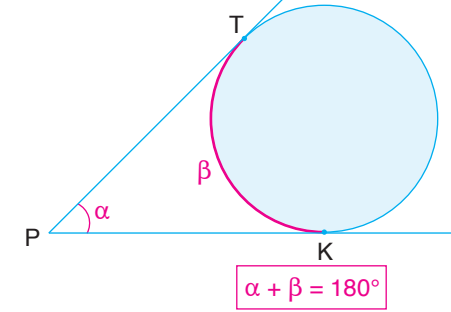
## 4 İç Açısı



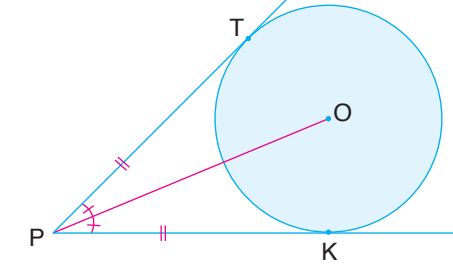
## 5 Dış Açısı



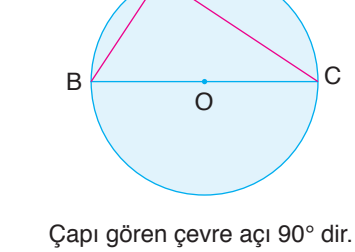
## 6



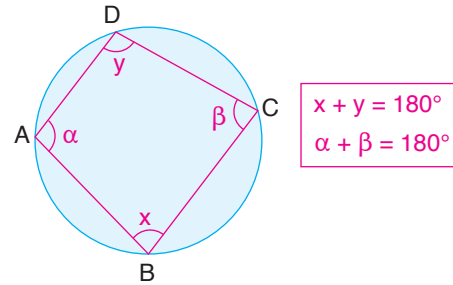
## 7



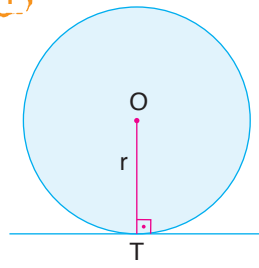
## 8



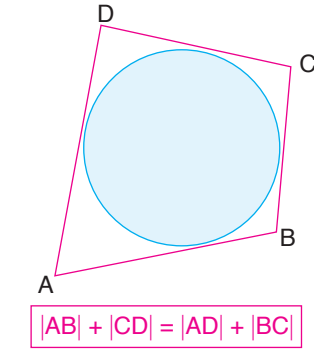
## 9 ABCD Kirişler Dörtgeni



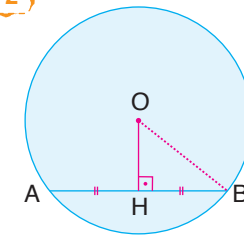
## 1



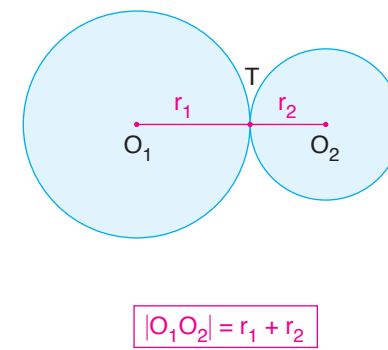
## 5 ABCD Teğetler Dörtgeni



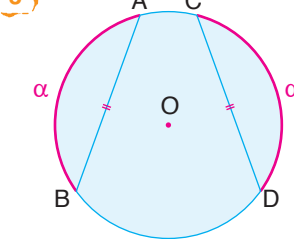
## 2



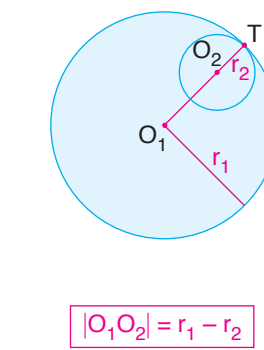
## 6 Dıştan Teğet Çemberler



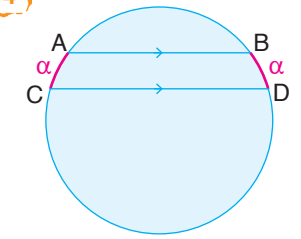
## 3



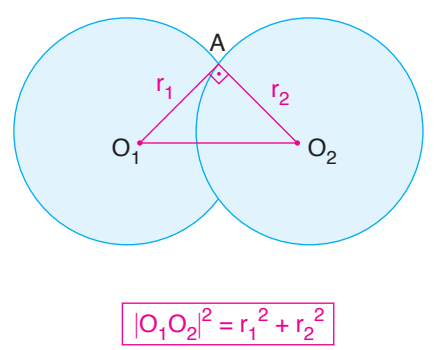
## 7 İçten Teğet Çemberler



## 4



## 8 Çemberler Dik Kesişirse



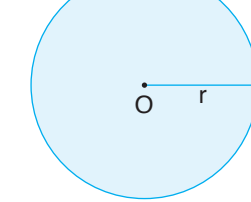
## ÇEMBERDE AÇI

## ÇEMBER VE DAİRE

## ÇEMBERDE UZUNLUK

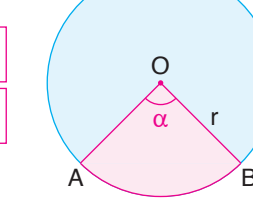
## DAİREDE UZUNLUK VE ALAN

## 1



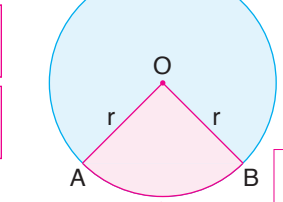
$$\begin{aligned} \text{Çevre} &= 2\pi r \\ \text{Alan} &= \pi r^2 \end{aligned}$$

## 2



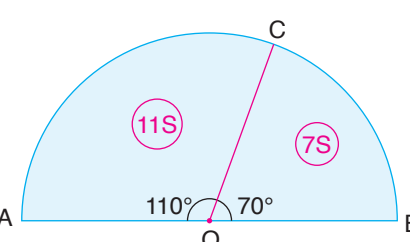
$$\begin{aligned} |AB| &= 2\pi r \cdot \frac{\alpha}{360^\circ} \\ \text{Dilim Alanı} &= \pi r^2 \cdot \frac{\alpha}{360^\circ} \end{aligned}$$

## 3

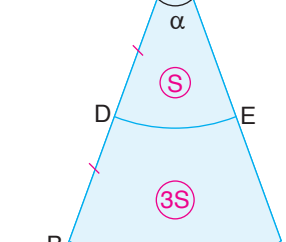


$$\text{Dilim Alanı} = \frac{l \cdot r}{2}$$

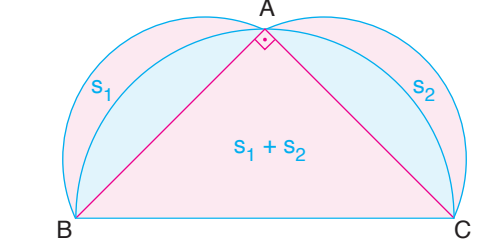
## 4



## 5



## 6





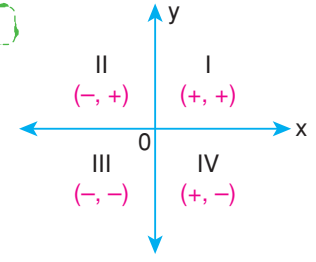
# ANALİTİK GEOMETRİ-1

## DOĞRU ANALİTİĞİ-1

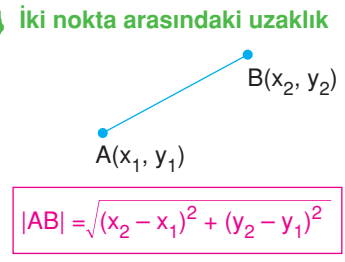
## NOKTA ANALİTİĞİ

## DOĞRU ANALİTİĞİ - 2

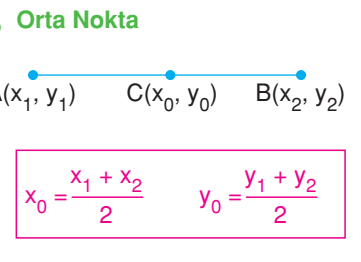
1



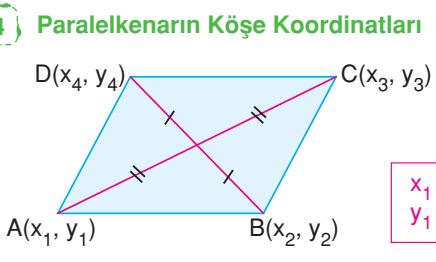
2



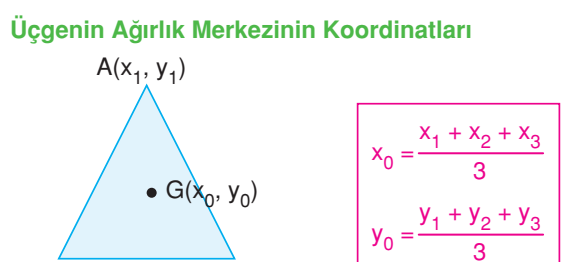
3



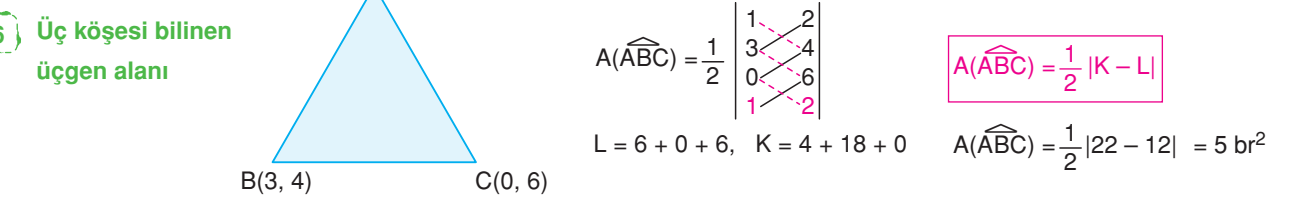
4



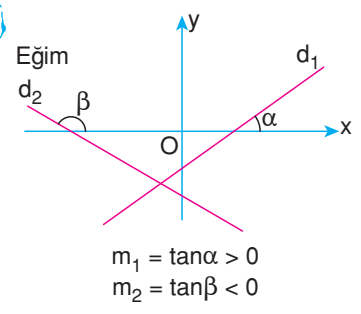
5



6



1



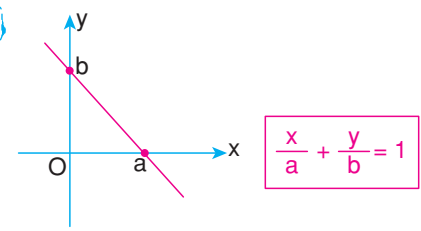
2

İki noktası bilinen doğrunun eğimi;  
A(x<sub>1</sub>, y<sub>1</sub>) ve B(x<sub>2</sub>, y<sub>2</sub>) noktaları için  $m = \frac{y_2 - y_1}{x_2 - x_1}$

3

Eğim ve bir noktası bilinen doğru denklemini  
(Kartezyen veya Kapalı Denklemler)  
Eğim m ve nokta A(x<sub>1</sub>, y<sub>1</sub>) için  
d:  $m = \frac{y - y_1}{x - x_1}$  şeklinde yazılır.

4



5

x eksenini y = 0 doğrusudur.  
y eksenini x = 0 doğrusudur.

6

Parametrik ve vektörel denklemler  
 $\vec{u} = (a, b)$   $\vec{u}$  doğrultman vektör  
A(x<sub>1</sub>, y<sub>1</sub>) d  $\vec{u} \parallel d$

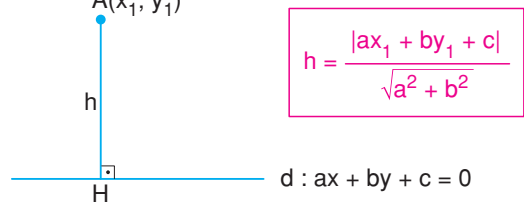
$x = x_1 + k \cdot a$   
 $y = y_1 + k \cdot b$  Parametrik denklem

$(x, y) = (x_1, y_1) + k \cdot (a, b)$  Vektörel denklem

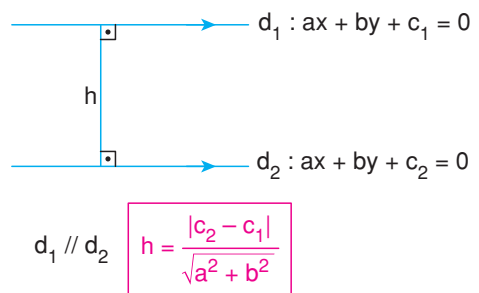
7

Paralel doğruların eğimleri eşittir.  
 $d_1 \parallel d_2 \Leftrightarrow m_1 = m_2$   
Dik doğruların eğimleri çarpımı -1'dir.  
 $d_1 \perp d_2 \Leftrightarrow m_1 \cdot m_2 = -1$

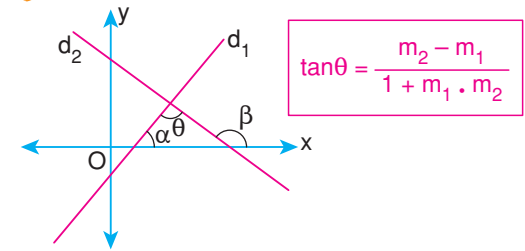
1 Noktanın doğruya uzaklığı



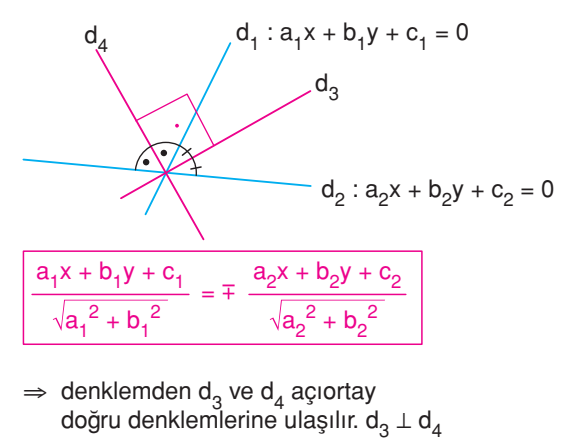
2 İki doğru arasındaki uzaklık



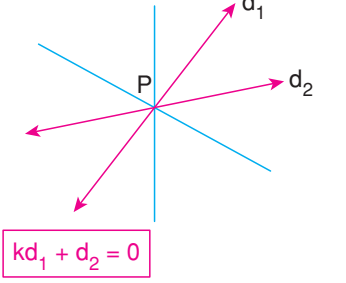
3 İki doğru arasındaki uzaklık



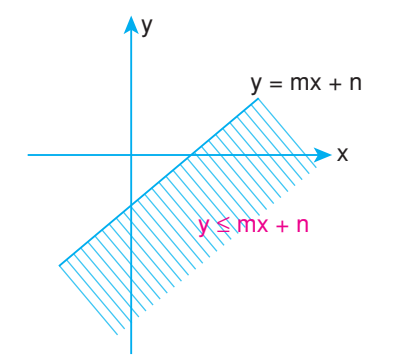
4 Açılırtay doğru denklemleri



5 Doğru demeti



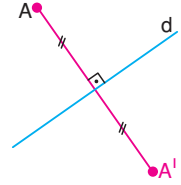
6 Eşitsizlik Grafiği



## 1 Noktanın noktaya göre simetriği



## 2 Noktanın doğruya göre simetriği

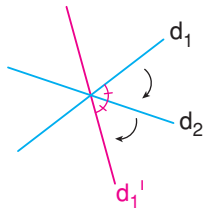


$A(x_1, y_1)$	Ox eksenine göre	$A'(x_1, -y_1)$
	Oy eksenine göre	$A'(-x_1, y_1)$
	Orijin	$A'(-x_1, -y_1)$
	$y = x$	$A'(y_1, x_1)$
	$y = -x$	$A'(-y_1, -x_1)$
	$x = a$	$A'(2a - x_1, y_1)$
	$y = b$	$A'(x_1, 2b - y_1)$

## 3 Doğrunun noktaya göre simetriği

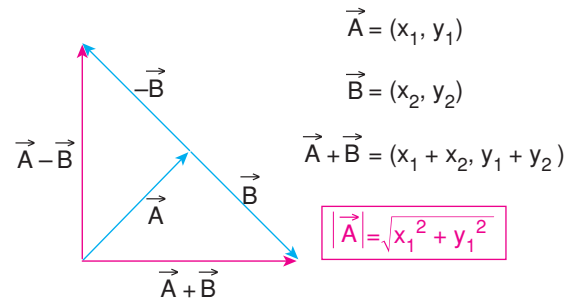


## 4 Doğrunun doğruya göre simetriği



$ax + by + c = 0$	Ox eksenine	$ax - by + c = 0$
	Oy eksenine	$-ax + by + c = 0$
	Orijin	$-ax - by + c = 0$
	$y = x$	$ay + bx + c = 0$
	$y = -x$	$-ay - bx + c = 0$
	$x = d$	$a(2d - x) + by + c = 0$
	$y = e$	$ax + b(2e - y) + c = 0$

## 1



## 4 Skaler Çarpım (Öklid İç Çarpımı)

$$\vec{A} = (x_1, y_1), \vec{B} = (x_2, y_2)$$

$$\vec{A} \cdot \vec{B} = x_1 \cdot x_2 + y_1 \cdot y_2$$

## 2

$$\vec{A} = (x_1, y_1), \vec{B} = (x_2, y_2)$$

$$\vec{AB} = \vec{B} - \vec{A} = (x_2 - x_1, y_2 - y_1)$$

Eşit vektörler  
 $\vec{A} = \vec{B} \Leftrightarrow x_1 = x_2, y_1 = y_2$

Vektörün bir reel sayı ile çarpımı  
 $k\vec{A} = (kx_1, ky_1)$

## 3

$\vec{A}$  vektörü ile aynı yönlü birim vektör,

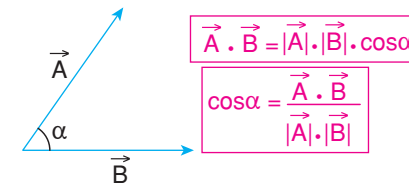
Vektörlerin paralellliği

$$\frac{x_1}{x_2} = \frac{y_1}{y_2}$$

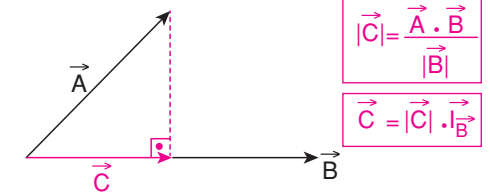
Vektörlerin dikliği;

$$x_1 \cdot x_2 + y_1 \cdot y_2 = 0$$

## 5 İç Çarpımın Geometrik Yorumu



## 6 Dik İzdüşüm Uzunluğu ve Vektörü



SİMETRİ (YANSIMA)

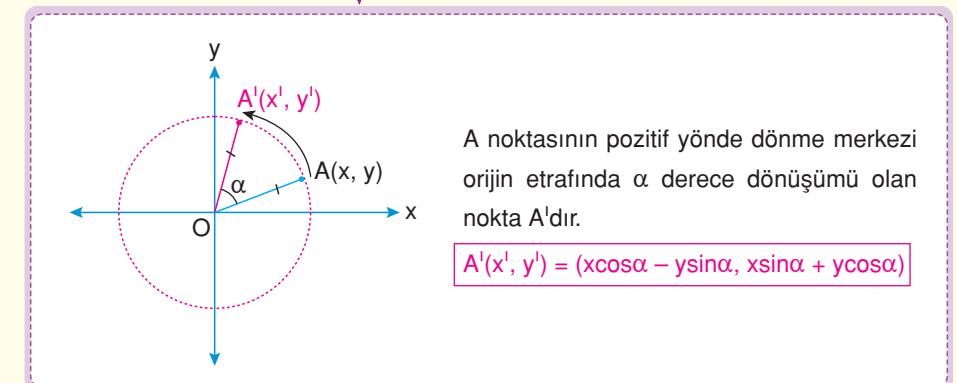
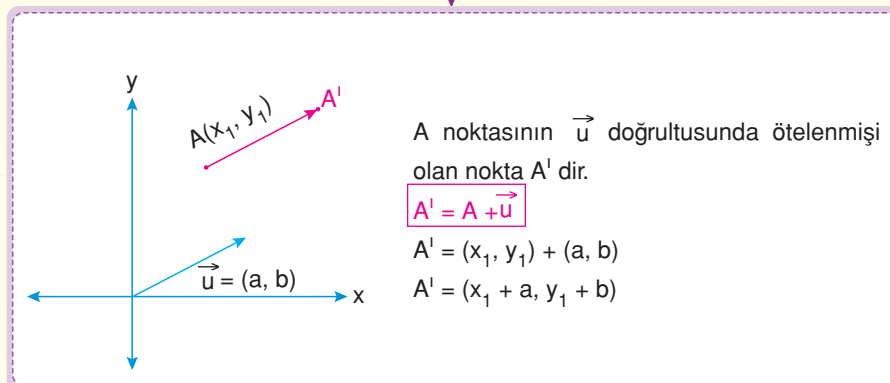
DÖNÜŞÜMLER

ÖTELEME

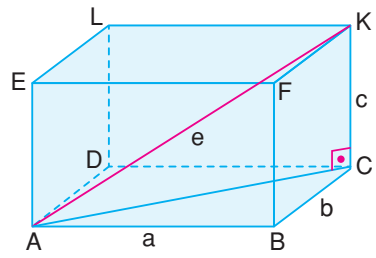
DÖNDÜRME

ANALİTİK GEOMETRİ - 2

VEKTÖRLER

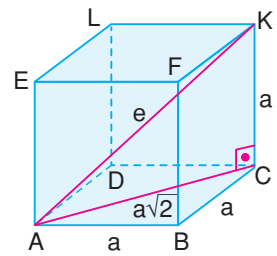


## 1 Dikdörtgenler Prizması



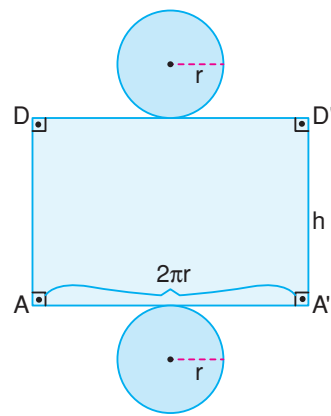
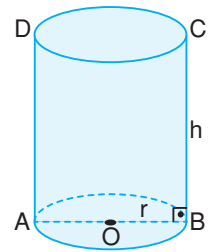
$$\begin{aligned} \text{Yanal Alan} &= 2(ac + bc) \\ \text{Alan} &= 2(ab + ac + bc) \\ \text{Hacim} &= a \cdot b \cdot c \\ e &= \sqrt{a^2 + b^2 + c^2} \end{aligned}$$

## 2 Küp



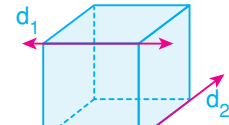
$$\begin{aligned} \text{Yanal Alan} &= 4a^2 \\ \text{Alan} &= 6a^2 \\ \text{Hacim} &= a^3 \\ e &= a\sqrt{3} \end{aligned}$$

## 3 Dik Silindir



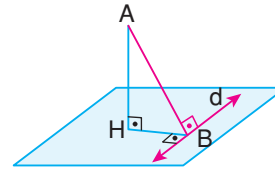
$$\begin{aligned} \text{Yanal Alan} &= 2\pi r \cdot h \\ \text{Alan} &= 2\pi r h + 2\pi r^2 \\ \text{Hacim} &= \pi r^2 \cdot h \end{aligned}$$

1  $\mathbb{R}^3$ 'de aykırı doğrular paralel değildir, kesişmez.

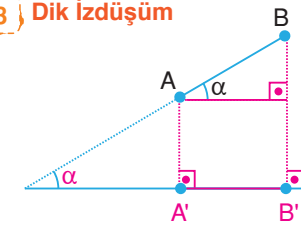


•  $d_1$  ve  $d_2$  aykırı doğrulardır.

## 2 Üç Dikme Teoremi



## 3 Dik İzdüşüm



$$|A'B'| = |AB| \cdot \cos \alpha$$

## UZAY GEOMETRİ

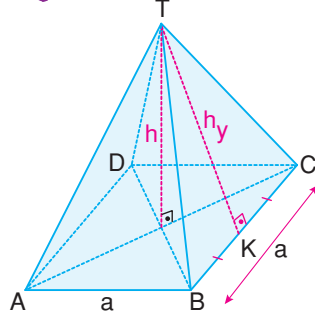
## UZAY GEOMETRİ VE KATI CİSİMLER

PRİZMA

KÜRE VE DÖNEL CİSİMLER

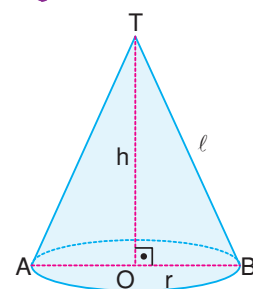
PİRAMİT

## 1 Düzgün Kare Dik Piramit



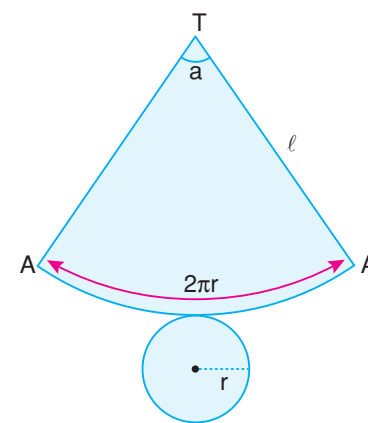
$$\begin{aligned} \text{Yanal Alan} &= 4 \cdot \frac{a \cdot h_y}{2} \\ \text{Alan} &= 4 \cdot \frac{a \cdot h_y}{2} + a^2 \\ \text{Hacim} &= \frac{1}{3} a^2 \cdot h \end{aligned}$$

## 2 Dik Koni



$$\text{Yanal Alan} = \pi r \ell$$

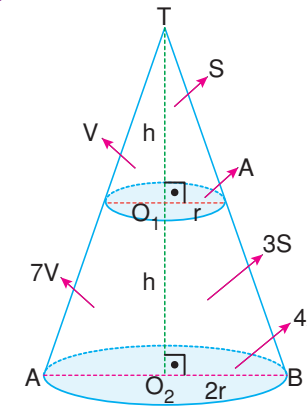
$$\text{Alan} = \pi r \ell + \pi r^2$$



$$\text{Hacim} = \frac{1}{3} \pi r^2 \cdot h$$

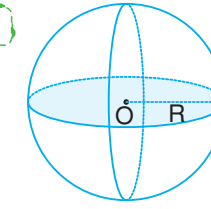
$$\frac{r}{\ell} = \frac{\alpha}{360^\circ}$$

## 3 Kesik Piramit



$$\begin{aligned} k = \frac{1}{2}, \quad k^2 = \frac{1}{4}, \quad k^3 = \frac{1}{8} \\ \downarrow \quad \downarrow \quad \downarrow \\ \text{uzunluk} \quad \text{alan} \quad \text{hacim} \\ \text{oranı} \quad \text{oranı} \quad \text{oranı} \\ r \quad A \quad V \\ 2r \quad 4A \quad 7V \end{aligned}$$

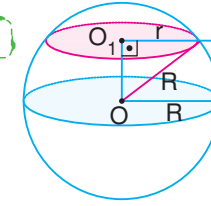
## 1



$$\text{Alan} = 4\pi R^2$$

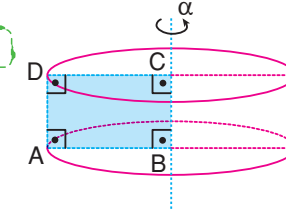
$$\text{Hacim} = \frac{4}{3} \pi R^3$$

## 2



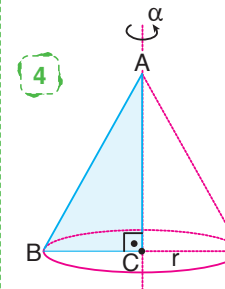
Küre düzlemde kesilirse oluşan kesit dairedir.

## 3



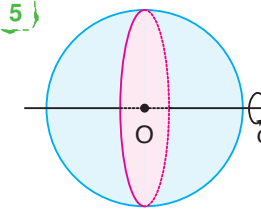
Dikdörtgen, kenarlarından biri etrafında  $\alpha = 360^\circ$  döndürülürse **dik silindir** oluşur.

## 4



Dik üçgen, dik kenarlarından biri etrafında  $\alpha = 360^\circ$  döndürülürse **dik koni** oluşur.

## 5



Daire, çap eksenini etrafında  $\alpha = 180^\circ$  döndürülürse **küre** oluşur.